

Chapter 9 / Example 41

Intersecting planes

Given the three planes $\pi_1 : 2x - 3y + 5z = 1$, $\pi_2 : x + 2y - z = 0$ and $\pi_3 : 2x + 4y - 2z = 1$, show that:

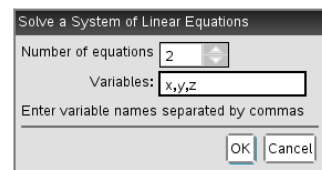
- a** $\pi_2 \parallel \pi_3$ **b** π_1 and π_2 intersect and find the equation of the line.

Open a new document and add a Calculator page.

Press **menu** 3:Algebra | 2:Solve System of Linear Equations...

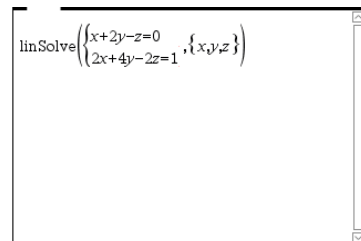
Select 2 equations and edit Variables by changing x, y to x, y, z .

Press **enter**.



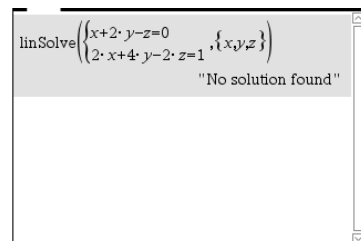
Solve the equations
$$\begin{cases} x + 2y - z = 0 \\ 2x + 4y - 2z = 1 \end{cases}$$

Type the equations and press **enter**.



The calculator displays no solution found.

If two planes do not intersect, then they must be parallel.



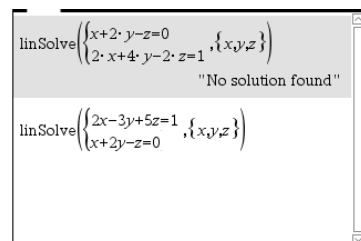
Press **menu** 3:Algebra | 2:Solve System of Linear Equations...

Select 2 equations and edit Variables by changing x, y to x, y, z .

Press **enter**.

Solve the equations
$$\begin{cases} 2x - 3y + 5z = 1 \\ x + 2y - z = 0 \end{cases}$$

Type the equations and press **enter**.

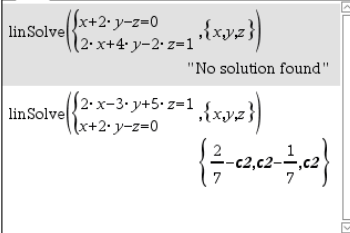


Chapter 9 / Example 41

Intersecting planes

The calculator displays the solution:

$$\begin{cases} x = \frac{2}{7} - \epsilon 2 \\ y = \epsilon 2 - \frac{1}{7} \\ z = \epsilon 2 \end{cases} \quad \text{or} \quad \begin{cases} x = \frac{2}{7} - \mu \\ y = -\frac{1}{7} + \mu \\ z = \mu \end{cases} \quad \text{or} \quad \frac{x - \frac{2}{7}}{-1} = \frac{y + \frac{1}{7}}{1} = \frac{z}{1}$$



$$\text{linSolve}\left(\begin{cases} x+2 \cdot y-z=0 \\ 2 \cdot x+4 \cdot y-2 \cdot z=1 \end{cases}, \{x, y, z\}\right)$$

"No solution found"

$$\text{linSolve}\left(\begin{cases} 2 \cdot x-3 \cdot y+5 \cdot z=1 \\ x+2 \cdot y-z=0 \end{cases}, \{x, y, z\}\right)$$

$$\left\{ \frac{2}{7} - \epsilon 2, \epsilon 2 - \frac{1}{7}, \epsilon 2 \right\}$$